

Problem Solving

- ⑤ Determine f_1 of a CLOSED-ended air column
 $L = 67.5 \text{ cm}$

$$L = \frac{1}{4} \lambda$$

$$67.5 \text{ cm} = \frac{1}{4} \lambda$$

$$\lambda = 270 \text{ cm}$$

$$v = \lambda f$$

$$340 \frac{\text{m}}{\text{s}} = (2.7 \text{ m}) f_1$$

$$f_1 = 126 \text{ Hz}$$

- ⑥ Determine Length of CLOSED ended air column required to produce a fundamental frequency of 480 Hz .

$$v = \lambda f$$

$$340 \text{ m/s} = \lambda (480 \text{ Hz})$$

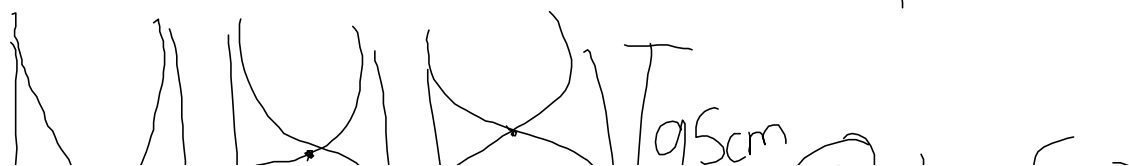
$$\lambda = 0.708 \text{ m}$$

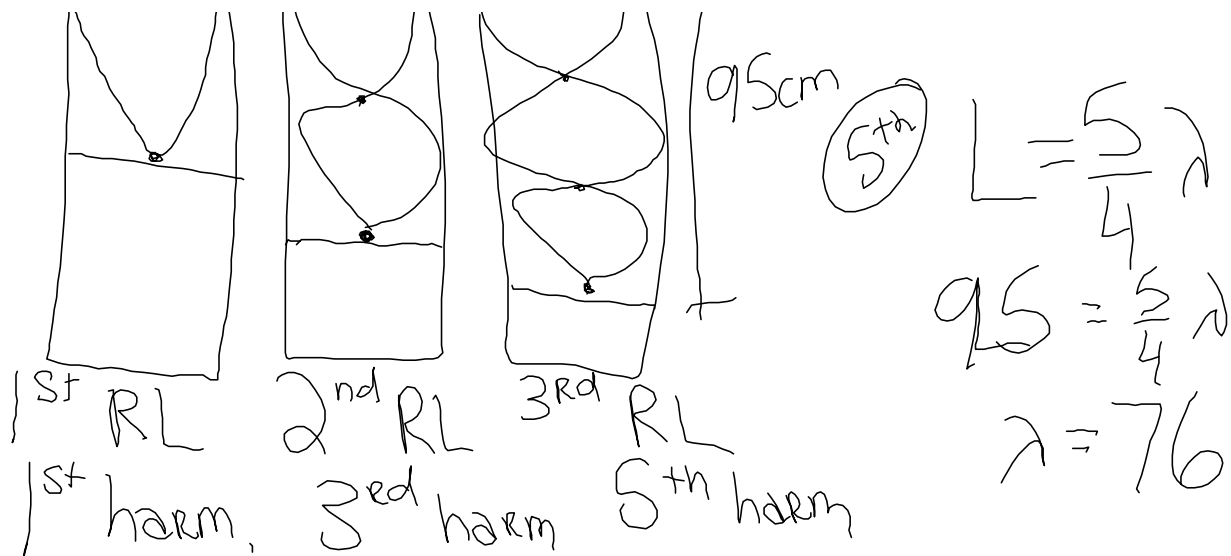
$$\lambda = 4L$$

$$0.708 = 4L$$

$$L = 0.177 \text{ m}$$

- ⑪ 3rd resonance length of closed air column = 95 cm . Determine 1st + 2nd





1st $L = \frac{1}{4} \lambda$
 $= \frac{1}{4} (76)$ $L = 19 \text{ cm}$

3rd $L = \frac{3}{4} \lambda$
 $= \frac{3}{4} (76)$ $L = 57 \text{ cm}$

17 85cm guitar string
 Speed of vibration = 332 m/s

13 $L_2 - L_1 = 20.2$
 $\lambda - \frac{1}{2} \lambda = 20.2$
 $\frac{1}{2} \lambda = 20.2$
 $\lambda = 40.4 \text{ cm}$

$$\lambda = 40.4 \text{ cm}$$

$$v = \lambda f$$

$$347 \text{ m/s} = (0.404 \text{ m}) f$$

$$f = 860 \text{ Hz}$$

Intensity of a sound wave

- Amount of energy transported past a given area of the medium per unit of time
- Watts/m²

$$\text{Intensity} = \frac{\text{Energy}}{\text{Time} \cdot \text{Area}} \quad \text{or} \quad \text{Intensity} = \frac{\text{Power}}{\text{Area}}$$

Sound level/Decibels

- The threshold of hearing is assigned a sound level of 0 decibels (abbreviated 0 dB); this sound corresponds to an intensity of $1 \cdot 10^{-12} \text{ W/m}^2$
- Scale based on powers of 10
- sound that is 10 times more intense ($1 \cdot 10^{-11} \text{ W/m}^2$) is assigned a sound level of 10 dB.
- A sound that is $10 \cdot 10$ or 100 times more intense ($1 \cdot 10^{-10} \text{ W/m}^2$) is assigned a sound level of 20 db.
- A sound that is $10 \cdot 10 \cdot 10$ or 1000 times more intense ($1 \cdot 10^{-9} \text{ W/m}^2$) is assigned a sound level of 30 db.
- A sound that is $10 \cdot 10 \cdot 10 \cdot 10$ or 10000 times more intense ($1 \cdot 10^{-8} \text{ W/m}^2$) is assigned a sound level of 40 db.

Source	Intensity	Intensity Level	# of Times Greater Than TOH
Threshold of Hearing (TOH)	$1 \cdot 10^{-12} \text{ W/m}^2$	0 dB	10^0
Rustling Leaves	$1 \cdot 10^{-11} \text{ W/m}^2$	10 dB	10^1
Whisper	$1 \cdot 10^{-10} \text{ W/m}^2$	20 dB	10^2
Normal Conversation	$1 \cdot 10^{-6} \text{ W/m}^2$	60 dB	10^6
Busy Street Traffic	$1 \cdot 10^{-5} \text{ W/m}^2$	70 dB	10^7
Vacuum Cleaner	$1 \cdot 10^{-4} \text{ W/m}^2$	80 dB	10^8
Large Orchestra	$6.3 \cdot 10^{-3} \text{ W/m}^2$	98 dB	$10^{9.8}$
Walkman at Maximum Level	$1 \cdot 10^{-2} \text{ W/m}^2$	100 dB	10^{10}
Front Rows of Rock Concert	$1 \cdot 10^{-1} \text{ W/m}^2$	110 dB	10^{11}
Threshold of Pain	$1 \cdot 10^1 \text{ W/m}^2$	130 dB	10^{13}
Military Jet Takeoff	$1 \cdot 10^2 \text{ W/m}^2$	140 dB	10^{14}
Instant Perforation of Eardrum	$1 \cdot 10^4 \text{ W/m}^2$	160 dB	10^{16}

octave - any two sounds whose frequencies make a 2:1 ratio are said to be separated by an **octave**

Interval	Frequency Ratio	Examples
Octave	2:1	512 Hz and 256 Hz
Third	5:4	320 Hz and 256 Hz
Fourth	4:3	342 Hz and 256 Hz
Fifth	3:2	384 Hz and 256 Hz

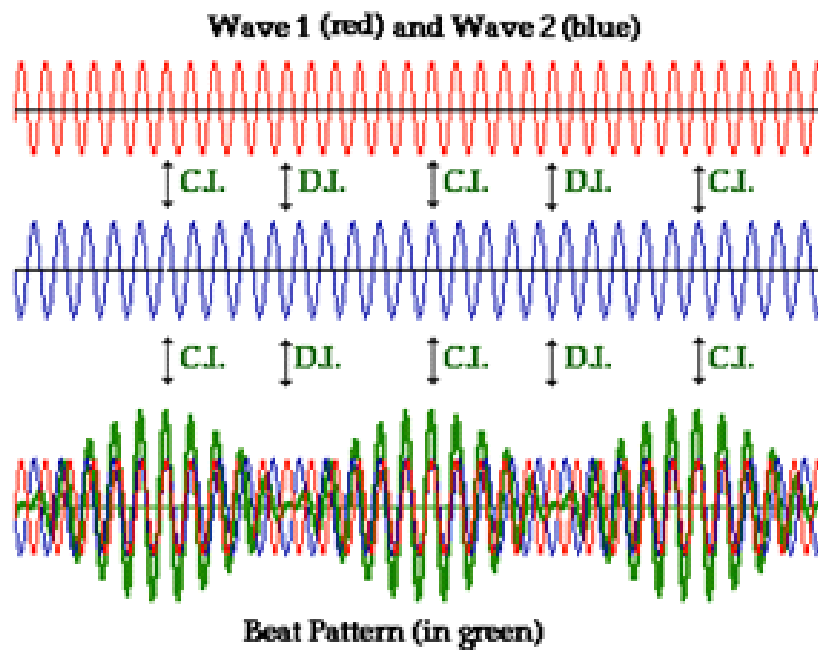
Example:

A musical note that is separated by an octave from middle C (256 Hz) has a frequency of: $\frac{512\text{ Hz}}{128\text{ Hz}}$



Beats

- **Beats** are the periodic and repeating fluctuations heard in the intensity of a sound when two sound waves of very similar frequencies interfere with one another.

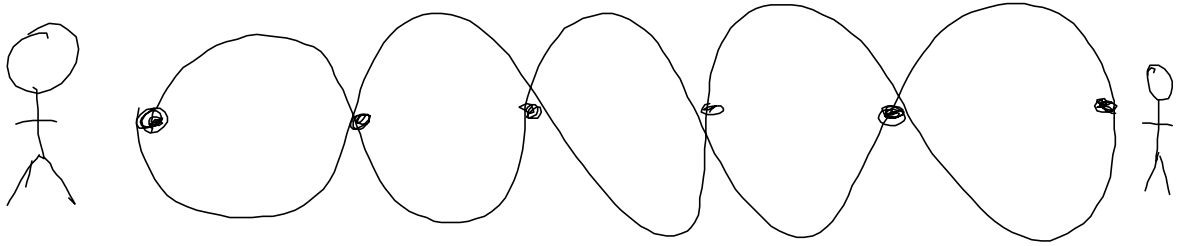


- beat frequency
 - rate at which the volume is heard to be oscillating from high to low volume
 - For example, if two complete cycles of high and low volumes are heard every second, the beat frequency is 2 Hz.
 - The beat frequency is always equal to the difference in frequency of the two notes that interfere to produce the beats.
- Longer Beats video:
<https://www.youtube.com/watch?v=8vUuGRaTQ2E>
- Shorter Beats video:
<https://www.youtube.com/watch?v=dD9gtq08tss>

consonance (pleasing sounds)

dissonance (unpleasant sounds)

$L = 6.0 \text{ m}$



5th harmonic

$$L = 5 \text{ cm} \quad r = 2.4 \text{ m}$$

$$f = \frac{85 \times \frac{1}{\text{min}}}{60 \text{ s}} = \frac{1.42}{\text{s}} = 1.42 \text{ Hz}$$

$$V = \lambda f = (2.4 \text{ m})(1.42 \text{ Hz})$$

$$V = 3.4 \text{ m/s}$$

$v = \lambda f$

Speed wavelength frequency (Hz)

Vibrations
Second

Speed
m/s

wavelength
metres

Vibrations
Second

— in air → speed
of sound

— in Rope → speed of
Rope